

B. Tech (CSE) (Sem-4th)**Discrete Structures****Sub Code: BTCS 402****Maximum Marks: 60**

Paper ID- A2305

Time: 3 hrs.**Instructions to the Candidates:**

- 1) Section A is compulsory carrying Ten Questions each of Two marks.
- 2) Section-B contains Five Questions carrying 5 Marks. Attempt any four questions.
- 3) Section-C contains Three Question carrying 10 Marks. Attempt any two questions.

Section-A

- Q1) a) Differentiate between Equal and Equivalent set?
b) What is function and what are its types.
c) Prove that If R is an equivalence relation on a set A. Show that R^{-1} is also an equivalence relation on A.
d) Give an example of a relation which is neither reflexive, nor symmetric, nor transitive and nor anti-symmetric.
e) $A(n) = A(n-1) + 2A(n-2)$ where $n \geq 3$ is a sequence of integer with basic values $A(1) = 1$, $A(2) = 1$. Find $A(5)$ by Recursion and Iterative Method?
f) Prove de-Morgan's Law: $a+b = \overline{\overline{a} \cdot \overline{b}}$
g) Prove that maximum degree of any vertex in a simple graph having n vertices is n-1.
h) Draw 3-regular graphs with nine vertices
i) Define Groups. Give example for the same
j) Prove by using Boolean algebra:
 $a+a' \cdot c = a+c$

Section -B

- Q2) If $A(n) - 6A(n-1) + 8A(n-2) = 0$ for $n \geq 2$ with, $A(0)=10$ and $A(1)=25$. Determine the sequence from its generating function.
- Q3. a) Give an example of Planar and non Planar graphs
b) What is Euler path and circuit? Give example?
- Q4) a) Draw on-off switching diagram of : $a[(b+\overline{d})+(\overline{c}(a+d+\overline{c}))]b$
b) Draw the gate diagram of : $(x1((x2 \overline{x3})+(\overline{x2} \overline{x3}))) + (\overline{x1} \overline{x2} \overline{x3})$
- Q5. a) What is monoid? Explain with example?
b) Prove that the set Z of integers form an Abelian Group w.r.t usual addition of integers i.e. $(Z, +, 0)$ is an Abelian Group.
- Q6. A class consists of 40 girls and 60 boys. In how many ways can a President , Vice President, Treasurer and Secretary be chosen if the treasurer must be a girl, the secretary must be a boy and a student may not hold more than one office?

Section -C

- Q7. a) Prove that in a graph the number of vertices of odd degree is even
b) Write the Dijkstra's Algorithm
c) What is Euler's Formula?
- Q8. a) Prove that if A is a set then identity function I on A is one -one onto
b) Give an example of a relation which is reflexive and transitive but not symmetric
c) Give an example of relation which is reflexive, symmetric, anti-symmetric and transitive.
- Q9: a) By finding generating function of sequence $s(n)$, find solution of recurrence relations:
 $S(n+2) - 7S(n+1) + 12S(n) = 0$ for $n \geq 0$ Given $S(0)=2$, $S(1)=5$
b) Prove De-Morgan's Law.