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Roll No. ....

Total No. of Questions: 09]

[Total No. of Pages: 03

# **Paper ID [A0459]**

(Please fill this Paper ID in OMR Sheet)

B.Tech. (Sem. - 3<sup>rd</sup>/4<sup>th</sup>)

MATHEMATICS - III (CS - 203/204)

Time: 03 Hours

Maximum Marks: 60

## Instruction to Candidates:

- Section A is Compulsory. 1)
- Attempt any Four questions from Section B. 2)
- Attempt any Two questions from Section C. 3)

#### Section - A

Q1)

 $(10 \times 2 = 20)$ 

- Discuss the relationships between limit, continuity and differentiation of a) a function.
- Define fundamental theorem of Integral Calculus. b)
- Distinguish between Trapezoidal and Simpson's  $\frac{1}{3}$ rd rule of numerical c) integration.
- Define analytic function and Cauchy-Riemann equations. d)
- Poles and residues of analytic functions. e)
- Define residue theorem of functions of complex variables. f)
- Explain the conditions for the existance of Laplace transform of a function. g)
- Define conformal mapping. h)
- By: Ddeveloperz Discuss the categorization of Laplace, wave and heat equations. i)
- State Rolle's theorem. j)

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# Section - B

 $(4\times 5=20)$ 

**Q2)** Determine the analytic function f(z)=u+iv if

$$u-v = \frac{\cos x + \sin x - e^{-y}}{2(\cos x - \cosh y)}$$

and 
$$f\left(\frac{\pi}{2}\right) = 0$$
.

*Q3*) Evaluate

$$\int \frac{z-3}{z^2+2z+5} dz$$

where C is the circle |z+i+1|=2.

**Q4)** An impulse I (kg - sec) is applied to a mass m attached to a spring having a spring constant k. The system is damped with damping constant  $\mu$ . The differential equation governing the phenomena is

$$m\frac{d^2x}{dt^2} + kx + \mu \frac{dx}{dt} = I \delta(x).$$

where  $\delta(x)$  is unit impulse function. Derive expression for displacement x(t) of the mass, assuming initial conditions x(0) = x'(0) = 0.

- **Q5)** Find the area included between the curves  $y^2(2a-x)=x^3$  and its asymptote.
- **Q6)** Employ Taylor's method to obtain approximate solution of y at x = 0.2 for the differential equation  $\frac{dy}{dx} = 2y + 3e^x$ , y(0) = 0.

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## Section - C

$$(2 \times 10 = 20)$$

**Q7)** Using Runge-Kutta method of order 4, compute y(0.2) and y(0.4) from

$$10\frac{dy}{dx} = x^2 + y^2$$
,  $y(0) = 1$ .

taking h = 0.1.

- **Q8)** A tightly stretched string of length l with fixed ends is initially in equilibrium position. It is set vibrating by giving each point a velocity  $v_0 \sin^3 \left( \frac{\pi x}{l} \right)$ . Find the displacement y(x,t), using separation of variable technique.
- Q9) Show that the transformation

$$w = z + \frac{a^2}{z}$$

transforms circles with origin at the centre in the z-plane into coaxial concentric, confocal ellipses in the w - plane.

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