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Roll No. Total No. of Questions : 09]

[Total No. of Pages : 03

Paper ID [A0459]

(Please fill this Paper ID in OMR Sheet)

B.Tech. (Sem. - 3rd/4th)

MATHEMATICS - III (CS - 203/204)

Time : 03 Hours

Q1)

Maximum Marks : 60

Instruction to Candidates:

- 1) Section A is Compulsory.
- 2) Attempt any Four questions from Section B.
- 3) Attempt any Two questions from Section C.

Section - A

$(10 \times 2 = 20)$

- a) Discuss the relationships between limit, continuity and differentiation of a function.
- b) Define fundamental theorem of Integral Calculus.
- c) Distinguish between Trapezoidal and Simpson's $\frac{1}{3}$ rd rule of numerical integration.
- d) Define analytic function and Cauchy-Riemann equations.
- e) Poles and residues of analytic functions.
- f) Define residue theorem of functions of complex variables.
- g) Explain the conditions for the existance of Laplace transform of a function.
- h) Define conformal mapping.
- i) Discuss the categorization of Laplace, wave and heat equations.
- j) State Rolle's theorem.

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P.T.O.

Section - B -

$$(4\times 5=20)$$

Q2) Determine the analytic function f(z) = u + iv if

$$u - v = \frac{\cos x + \sin x - e^{-y}}{2(\cos x - \cosh y)}$$

and $f\left(\frac{\pi}{2}\right) = 0.$

Q3) Evaluate

$$\int_{C} \frac{z-3}{z^2+2z+5} dz$$

where C is the circle |z+i+1|=2.

Q4) An impulse I (kg - sec) is applied to a mass *m* attached to a spring having a spring constant *k*. The system is damped with damping constant μ . The differential equation governing the phenomena is

$$m\frac{d^2x}{dt^2} + kx + \mu\frac{dx}{dt} = I\delta(x).$$

where $\delta(x)$ is unit impulse function. Derive expression for displacement x(t) of the mass, assuming initial conditions x(0) = x'(0) = 0.

- **Q5)** Find the area included between the curves $y^2(2a-x) = x^3$ and its asymptote.
- **Q6)** Employ Taylor's method to obtain approximate solution of y at x = 0.2 for the differential equation $\frac{dy}{dx} = 2y + 3e^x$, y(0) = 0.

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Section - C

 $(2 \times 10 = 20)$

Q7) Using Runge-Kutta method of order 4, compute y(0.2) and y(0.4) from

$$10\frac{dy}{dx} = x^2 + y^2, \ y(0) = 1.$$

taking h = 0.1.

Q8) A tightly stretched string of length *l* with fixed ends is initially in equilibrium position. It is set vibrating by giving each point a velocity $v_0 \sin^3 \left(\frac{\pi x}{l}\right)$. Find

the displacement y(x,t), using separation of variable technique.

Q9) Show that the transformation

$$w = z + \frac{a^2}{z}$$

transforms circles with origin at the centre in the z-plane into coaxial concentric, confocal ellipses in the w - plane.

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