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Total No. of Questions: 091

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B.Tech. (Sem. - 3rd/4th) **MATHEMATICS - III**

SUBJECT CODE: CS - 203/204 (2K2 Batch)

Paper ID: [A0457]

[Note: Please fill subject code and paper ID on OMR]

Time: 03 Hours

Maximum Marks: 60

Instruction to Candidates:

- 1) Section - A is **Compulsory**.
- Attempt any **Four** questions from Section B. 2)
- Attempt any Two questions from Section C. 3)

Section - A

Q1)

$$(10 \times 2 = 20)$$

- Verify Rolle's theorem for the function $f(x) = x^2 5x + 4$ in the interval a) $1 \le x \le 4$.
- Find the Laplace transform of $f(t) = \sqrt{t} e^{3t}$ b)
- Give an example of bilinear transformation. c)
- Prove that $\underset{x\to a}{\text{Lt}}(x-a)\sin\frac{1}{x-a}=0$. d)
- y: Ddeveloperz State the Taylor's theorem with Lagrange's form of remainder. e)
- Give the statement of Cauchy Riemann equations. f)
- Using Picard's method find first approximation of $\frac{dy}{dx} = x + y^2$, y(0) = 1g)
- h) Write the necessary and sufficient conditions for Riemann's integration.
- Evaluate $\int_{0}^{1} dx \int_{0}^{x} e^{\frac{y}{x}} dy$. i)
- Evaluate $\oint \frac{e^{-z}}{z+1} dz$, where C is the circle |z| = 2. j)

Section - B

$$(4 \times 5 = 20)$$

- Q2) Find the volume of tetrahedron bounded by the co-ordinate planes and the plane $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$.
- Q3) Find the sum of the residues of the function $f(z) = \frac{\sin z}{z \cos z}$ at its poles inside the circle |z| = 2.
- Q4) Using convolution theorem, find the inverse of $\frac{s+2}{(s^2+4s+5)^2}$.
- Q5) Using Fourier sine integral, show that

$$\int_{0}^{\infty} \frac{1 - \cos \pi \lambda}{\lambda} \sin x \lambda \, d\lambda = \begin{cases} \frac{1}{2} \pi, & \text{when } 0 < x < \pi \\ 0, & \text{when } x > \pi \end{cases}$$

Q6) Find the entire length of the cardioid $r = a(1 + \cos\theta)$.

Section - C

$$(2 \times 10 = 20)$$

- Q7) Using Runge Kutta method of order 4, find y(0.1) and y(0.2) given that $\frac{dy}{dx} = x^2 y, y(0) = 1. \text{ (Take } h = 0.2\text{)}$
- Q8) Find the Laurent series of $f(z) = \frac{1}{(z-1)(z-2)}$ for the following intervals
 - (a) 1 < |z| < 2 (b) |z| > 2
- Q9) (a) A tightly stretched string with fixed end points x = 0 and x = L is initially in a position given by f(x). The initial velocity is zero, where

$$f(x) = \begin{cases} \frac{2K}{L}x & 0 \le x \le \frac{L}{2} \\ \frac{2K}{L}(L-x) & \frac{L}{2} < x < L \end{cases}$$

Obtain the displacement at any point *x* and any time *t*. (use wave equation).

(b) Find the values of a, b, c, d so that the function f(x) is analytic. where $f(z) = (x^2 + axy + by^2) + i(cx^2 + dxy + y^2)$