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Roll No.

Total No. of Pages : 02

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B.Tech.(2008-2010 Batches) (Sem.-1) ENGINEERING MATHEMATICS-I Subject Code : AM-101 Paper ID : [A0111]

Time : 3 Hrs.

Max. Marks : 60

INSTRUCTIONS TO CANDIDATES :

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION B & C. have FOUR questions each.
- 3. Attempt any FIVE questions from SECTION B & C carrying EIGHT marks each.
- 4. Select atleast TWO questions from SECTION B & C.

SECTION - A

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- I. Solve the following
 - (a) State De-Moivre's theorem.

(b) Prove that
$$i^{i} = e^{-(4n+1)\frac{\pi}{2}}$$

(c) Define Cauchy's Integral Test.

(d) Show that
$$\int_{0}^{\infty} \frac{1}{x^{7/4}} e^{-\sqrt{x}} dx = \frac{8}{3}\sqrt{\pi}$$
.

(e) Write an equation for ellipsoid.

(f) If
$$u = \frac{yz}{x}, v = \frac{zx}{y}, w = \frac{xy}{z}$$
. Find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$

- (g) Find the equation of the tangent plane and the normal to $xyz = a^2$ at (x_1, y_1, z_1) .
- (h) Find the area of the circle of radius *r*.
- (i) Define Uniform Convergence.
- (j) Expand $x^2y + 3y 2$ in powers of x 1 and y + 2 using Taylor's theorem.

[M - 54001]

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SECTION - B

- 2. Trace the curve, $y^2 = (x + 1)^3$.
- 3. Find the whole length of the curve, $x^{2/3} + y^{2/3} = a^{2/3}$.
- 4. If $u = \csc^{-1} \left(\frac{x^{1/2} + y^{1/2}}{x^{1/3} + y^{1/3}} \right)^{1/2}$, then prove that

$$x^{2} \frac{\partial^{2} u}{\partial x^{2}} + 2xy \frac{\partial^{2} u}{\partial x \partial y} + y^{2} \frac{\partial^{2} u}{\partial y^{2}} = \frac{\tan u}{12} \left(\frac{13}{12} + \frac{\tan^{2} u}{12} \right).$$

5. Find the point on the surface $z^2 = xy + 1$ nearest to the origin.

SECTION - C

6. Find the equation of the cone whose vertex is at origin and guiding curve is

$$\frac{x^2}{4} + \frac{y^2}{9} + \frac{z^2}{1} = 1, x + y + z = 1.$$

- 7. Find the volume of the ellipsoid $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1.$ 8. Test the convergence of the series $\frac{x}{1} + \frac{1}{2} \cdot \frac{x^3}{3} + \frac{1}{2} \cdot \frac{3}{4} \cdot \frac{x^5}{5} + \dots \infty.$
- 9. Prove that the *nth* roots of unity form the geometric progression. Also show that the sum of these *n* roots is zero and their product is $(-1)^{n-1}$.