

Roll No.

Total No. of Pages : 02

Total No. of Questions : 09

**B.Tech.(CE/ECE/EE/Electrical & Electronics/  
Electronics & Computer Engg./Electronics & Electrical/ETE)  
(2011 Onwards)  
B.Tech.(Electrical Engg. & Industrial Control) (2012 Onwards)  
(Electronics Engg.) (2012 Onwards)  
(Sem.-3)**

**ENGINEERING MATHEMATICS – III**

Subject Code : BTAM-301

Paper ID : [A1128]

Time : 3 Hrs.

Max. Marks : 60

**INSTRUCTIONS TO CANDIDATES :**

1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

**SECTION-A**

1) Write briefly :

- a) Define even and odd functions. Give an example of a function which is neither even nor odd.
- b) Write the sufficient conditions for the existence of Laplace transform.
- c) Find the Fourier series of the function  $f(x) = x, -\pi < x < \pi$ .
- d) Let  $f(t)$  satisfies the conditions of the existence theorem of Laplace transform and  $\mathbb{L}[f(t)] = \mathbb{F}(s)$ . Then which of the following is true
  - i)  $\lim_{s \rightarrow \infty} \mathbb{F}(s) \neq 0$ .
  - ii)  $\lim_{s \rightarrow \infty} s \mathbb{F}(s)$  is bounded.
- e) Classify the singular points of the following equation  $x^2y'' + axy' + by = 0$ , where  $a, b$  are constants.
- f) Show that  $P_n(1) = 1$ , where  $P_n(x)$  denotes the Legendre Polynomial.
- g) Eliminate the arbitrary constants  $a$  and  $b$  from  $z = ax + by + a^2b^2$ , to obtain the partial differential equation.

h) Classify the following partial differential equations :

i)  $u_{xx} - 2u_{xy} + u_{yy} = 0$

ii)  $xu_{xx} - yu_{xy} = 0$ .

i) Using the definition of limits, show that  $\lim_{z \rightarrow \infty} \frac{1}{z^2} = 0$ .

j) Compute the residue at all singular points of the function  $f(z) = \cot z$ .

### SECTION-B

2) Find the Fourier series of the function :

$$f(x) = \begin{cases} -k, & \text{if } -2 < x < 0 \\ k, & \text{if } 0 < x < 2 \end{cases}$$

3) Find  $L^{-1} \left[ \log \left( 1 + \frac{\omega^2}{s^2} \right) \right]$ , where the symbol  $\mathbb{L}^{-1}$  denotes inverse Laplace transform.

4) Using the recurrence relation  $(n + 1)P_{n+1}(x) = (2n + 1)xP_n(x) - nP_{n-1}(x)$  recursively, evaluate  $P_2(1.5)$  and  $P_3(2.1)$ .

5) Show that the function  $f(z) = \begin{cases} \frac{x^3(1+i) - y^3(1-i)}{x^2 + y^2}, & z \neq 0 \\ 0, & z = 0 \end{cases}$  satisfies the Cauchy-

Riemann equations at  $z = 0$  but  $f'(0)$  does not exist.

6) Using the method of separation of variables, solve the parabolic partial differential equation  $\frac{\partial^2 u}{\partial x^2} = 16 \frac{\partial u}{\partial y}$ .

### SECTION-C

7) If  $f(z) = u + iv$  is an analytic function of  $z = x + iy$  and  $u - v = e^{-x}[(x - y) \sin y - (x + y) \cos y]$ , then find  $u$ ,  $v$  and the analytic function  $f(z)$ .

8) Solve the following initial value problem using Laplace transform

$$4y'' - 8y' + 3y = \sin t, y(0) = 0, y'(0) = 2.$$

9) An elastic string of length  $l$  which is fastened at its ends  $x = 0$  and  $x = l$  is picked up at its center point  $x = \frac{l}{2}$  to a height of  $\frac{l}{2}$  and released from rest. Find the displacement of the string at any instant of time.