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Roll No. Total No. of Pages: 03

Total No. of Questions: 09

B.Tech. (2011 Onwards) (Sem.-2)
ENGINEERING MATHEMATICS - II

Subject Code: BTAM-102 Paper ID: [A1111]

Time: 3 Hrs. Max. Marks: 60

INSTRUCTIONS TO CANDIDATES:

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION B & C. have FOUR questions each.
- 3. Attempt any FIVE questions from SECTION B & C carrying EIGHT marks each.
- 4. Select atleast TWO questions from SECTION B & C.

SECTION A

1. Write briefly:

- a) Define Linear independent and dependent vectors.
- b) Find the characteristic equation of the matrix $\begin{pmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{pmatrix}$.
- c) Test whether the matrix $\begin{pmatrix} 1 & 0 & 0 \\ 0 & 3 & -1 \\ 0 & -1 & 3 \end{pmatrix}$ is diagonalisable or not?
- d) Express $\sin^5 \theta$ in terms of the sines of multiples of θ .
- e) Find the general and principle value of i^{i} .
- f) Examine the convergence / divergence of the series $\sum_{n=1}^{\infty} \frac{1}{(1+\frac{1}{n})^{n^2}}$.
- g) Define the term absolute convergence and use this concept to test the convergence of the series $\sum_{n=1}^{\infty} \frac{\sin n}{n^2}$.

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h) Find the degree and order of the differential equation
$$\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{3}{2}} = \frac{d^2y}{dx^2}$$

- i) For what value of k the equation $xy^3dx + k(x^2y^2)dy = 0$ is a exact equation.
- j) Find the complete solution of the equation :

$$\frac{d^2x}{dt^2} + 5\frac{dx}{dt} + 6x = 0, \text{ given } x(0) = 0, \frac{dx}{dt} (\text{at } t = 0) = 15.$$

SECTION-B

- 2. a) Use method of variation of parameters to find the general solution of the differential equation $y'' + y = \csc x$.
 - b) Find the complete solution of the differential $y'' 2y' + y = x \sin x$.
- 3. a) Solve the following simultaneous differential equation

$$\frac{dx}{dt} + y + 5x = e^t, \frac{dy}{dt} + x + 5y = e^5$$

- b) Find the complete solution of the differential equation $x^2y'' 3xy' + 5y = x \log x$ by using operator method.
- 4. a) Solve the differential equation : $\frac{dy}{dx} = \frac{y+1}{(y+2)e^x x}$
 - b) Find the particular solution of the differential equation $y'' 2y' + 2y = e^x \tan x$
- 5. An electric circuit consists of an inductance 0.1 henry, a resistance of 20 ohms, and a condenser of capacitance 25 microfarads. Find the charge q and the current i at time t, given the initial conditions q = 0.05 coulombs, i = 0 when t = 0.

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SECTION-C

- 6. a) Use the rank method to test the consistency of the system of equations x + 2y + z = 2; 3x + y 2z = 1; 4x 3y z = 3; 2x + 4y + 2z = 4, if consistent, then solve it completely.
 - b) Use Gauss-Jordan method to find the inverse of the matrix

$$\begin{pmatrix} 1 & 0 & 2 \\ 2 & -1 & 3 \\ 4 & 1 & 5 \end{pmatrix}$$

7. a) Verify Cayley-Hamilton theorem for the matrix

$$\begin{pmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{pmatrix}$$

and hence find its inverse.

- b) Prove that eigen values of Hermetian matrix are real.
- 8. a) Test the convergence of the series

$$\frac{x}{1.2} + \frac{x^2}{3.4} + \frac{x^3}{5.6} + \dots \infty (x > 0)$$

b) Test for what values of x does the series convergence/diverge?

$$\sum_{n=1}^{\infty} \frac{(n+1)^n}{n^{n+1}} x^n$$

9. a) Use Demoivre's theorem to prove that

$$\left(\frac{1+\sin\alpha+i\cos\alpha}{1+\sin\alpha-i\cos\alpha}\right)^n = \cos\left(\frac{n\pi}{2}-n\alpha\right)+i\sin\left(\frac{n\pi}{2}-n\alpha\right)$$

b) Separate $tan^{-1} (e^{i\theta})$ into real and imaginary parts.