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Roll No. Total No. of Pages: 02

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B.Tech.(CE/ECE/EE/Electrical & Electronics/ Electronics & Computer Engg./Electronics & Electrical/ETE) (2011 Onwards)

B.Tech.(Electrical Engg. & Industrial Control) (2012 Onwards) (Electronics Engg.) (2012 Onwards) (Sem.-3)

# **ENGINEERING MATHEMATICS - III**

Subject Code: BTAM-301 Paper ID: [A1128]

Time: 3 Hrs. Max. Marks: 60

## **INSTRUCTIONS TO CANDIDATES:**

- SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION-B contains FIVE questions carrying FIVE marks each and students have to attempt any FOUR questions.
- 3. SECTION-C contains THREE questions carrying TEN marks each and students have to attempt any TWO questions.

#### **SECTION-A**

### 1) Write briefly:

- a) Define even and odd functions. Give an example of a function which is neither even nor odd
- b) Write the sufficient conditions for the existence of Laplace transform.
- c) Find the Fourier series of the function  $f(x) = x, -\pi < x < \pi$ .
- d) Let f(t) satisfies the conditions of the existence theorem of Laplace transform and

 $\mathbb{L}[f(t)] = \mathbb{F}(s)$ . Then which of the following is true

- i)  $\lim_{s\to\infty} \mathbb{F}(s) \neq 0$ .
- ii)  $\lim_{s\to\infty} s \mathbb{F}(s)$  is bounded.
- e) Classify the singular points of the following equation

 $x^2y'' + axy' + by = 0$ , where a, b are constants.

- f) Show that  $P_n(1) = 1$ , where  $P_n(x)$  denotes the Legendre Polynomial.
- g) Eliminate the arbitrary constants a and b from  $z = ax + by + a^2b^2$ , to obtain the partial differential equation.

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- h) Classify the following partial differential equations:
  - i)  $u_{xx} 2u_{xy} + u_{yy} = 0$
  - ii)  $xu_{xx} yu_{xy} = 0$ .
- i) Using the definition of limits, show that  $\lim_{z\to\infty} \frac{1}{z^2} = 0$ .
- i) Compute the residue at all singular points of the function  $f(z) = \cot z$ .

## SECTION-B

2) Find the Fourier series of the function:

$$f(x) = \begin{cases} -k, & \text{if } -2 < x < 0 \\ k, & \text{if } 0 < x < 2 \end{cases}$$

- $f(x) = \begin{cases} -k, & \text{if } -2 < x < 0 \\ k, & \text{if } 0 < x < 2 \end{cases}$  Find  $L^{-1} \left[ \log \left( 1 + \frac{\omega^2}{s^2} \right) \right]$ , where the symbol  $\mathbb{L}^{-1}$  denotes inverse Laplace transform.
- Using the recurrence relation  $(n + 1)P_{n+1}(x) = (2n + 1)xP_n(x) nP_{n-1}(x)$  recursively, 4)
- Show that the function  $f(z) = \begin{cases} \frac{x^3(1+i) y^3(1-i)}{x^2 + y^2}, & z \neq 0 \\ 0, & z = 0 \end{cases}$  satisfies the Cauchy-Riemann equations of z = 0.15)

Riemann equations at z = 0 but f'(0) does not exist

Using the method of separation of variables, solve the parabolic partial differential 6) equation  $\frac{\partial^2 u}{\partial r^2} = 16 \frac{\partial u}{\partial v}$ .

## **SECTION-C**

- If f(z) = u + iv is an analytic function of z = x + iy and  $u v = e^{-x}[(x y)]$ 7)  $\sin y - [(x + y)\cos y]$ , then find u, v and the analytic function f(z).
- 8) Solve the following initial value problem using Laplace transform  $4y'' - 8y' + 3y = \sin t$ , y(0) = 0, y'(0) = 2.
- 9) An elastic string of length l which is fastened at its ends x = 0 and x = l is picked up at its center point  $x = \frac{1}{2}$  to a height of  $\frac{1}{2}$  and released from rest. Find the displacement of the string at any instant of time.

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