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Roll No.								Total No. of Pages : 3
Total No. of Questions : 09								

Questions

B.Tech. (Sem.-2) ENGINEERING MATHEMATICS-II Subject Code : AM-102 (2005 - 2010 Batch) Paper ID : [A0119]

Time: 3 Hrs.

Max. Marks : 60

INSTRUCTION TO CANDIDATES :

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION-B contains FIVE questions carrying FIVE marks each and students has to attempt any FOUR questions.
- SECTION-C contains THREE questions carrying TEN marks each and 3. students has to attempt any TWO questions.

SECTION-A

- 1. Write short notes on
 - a) Define rank of a matrix. What could be the maximum value of a rank of a 3×4 matrix?
 - b) Derive the condition for the linear transformation Y = AX to be orthogonal, where A is a square matrix.
 - c) What is necessary and sufficient condition for a differential equation Mdx + Ndv = 0 to be exact ?
 - d) Find the particular integral of the differential equation

 $(D^{3}+4D)y = \sin 2x$.

- e) Consider an electric circuit containing an inductance L and capacitance C. Let i be the current and q the charge in the condenser plate at any time t. Write down the differential equation of charge for this circuit. What is the nature of this differential equation ?
- f) Show that the vector $3y^4z^2\hat{i} + 4x^3z^2\hat{j} + 3x^2y^2\hat{k}$ is solenoidal.
- g) State Green's theorem in plane.

[N-2-1373]

- h) Show that the vector field $\vec{F} = (x^2 y^2 + x)\hat{i} (2xy + y)\hat{j}$ is irrotational.
- i) Define the terms 'Exhaustive events' and 'Mutually exclusive events'.
- j) Write a short note on 'objectives of sampling'.

SECTION-B

2. a) Reduce the following matrix to normal form and hence find its rank:

$$A = \begin{bmatrix} 8 & 1 & 3 & 6 \\ 0 & 3 & 2 & 2 \\ -8 & -1 & -3 & 4 \end{bmatrix}$$

b) Test the following system of equations for consistency and solve.

$$2x - 3y + 7z = 5$$
; $3x + y - 3z = 13$; $2x + 19y - 47z = 32$.

3. Find complete solutions of the following differential equations:

a)
$$(x^2y^2 + xy + 1)ydx + (x^2y^2 - xy + 1)xdy = 0$$

b)
$$p^2 + 2py \cot x = y^2$$

4. a) Find a complementary function and particular integral of the differential equation

$$\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = e^{e^x}$$

b) Find complete solution of the differential equation :

$$x^{3} \frac{d^{3}y}{dx^{3}} + 2x^{2} \frac{d^{2}y}{dx^{2}} + 2y = 10\left(x + \frac{1}{x}\right)$$

NNNN X

5. An elastic string of natural length 'a' is fixed at one end and a particle of mass 'm' hangs freely from the other end. The modulus of elasticity is 'mg'. The particle is pulled down a further distance 'l' below its equilibrium position and released from rest. Show that the motion of the particle is simple harmonic and find the periodicity.

SECTION-C

- 6. a) Find the directional derivative of φ(x, y, z) = x²yz + 4xz² at the point (1, -2, -1) in the direction of the vector 2 i j 2k.
 b) If F = (5xy-6x²) i + (2y 4x) j evaluate ∫_C F d d along the curve C in the XY-plane, y = x³ from the point (1,1) to (2,8).
 7. a) Verify Green's theorem for ∫_C [(3x 8y²)dx + (4y 6xy)dy] where C is the boundary of the region bounded by x = 0, y = 0 and x + y = 1.
 b) Apply Stoke's theorem ∮_C (yzdx + zxdy + xydz) where C is the curve x² + y² = 1, z = y².
- 8. a) Show that the function defined as under is a density function

$$f(x) = \begin{cases} e^{-x}, & x \ge 0\\ 0, & x < 0 \end{cases}$$

Determine the probability that the variate having this density will fall in the interval (1, 2). Also find the cumulative probability function F(2).

b) Fit a parabola $y = a + bx + cx^2$ to the following data :

x:246810y:3.0712.8531.4757.3891.29.

- 9. a) A die was thrown 9000 times and a throw of 5 or 6 was obtained 3240 times. On the assumption of random throwing, do the data indicate an unbiased die ?
 - b) The nine items of a sample have the following values: 45, 47, 50, 52, 48, 47, 49, 53, 51. Does the mean of these differ significantly from the assumed mean of 47.5 ?