Total no of pages :3 Total No. of Qustions :09

B.Tech (Sem.1st)

# ENGINEERING MATHEMATICS-I Subject Code :BTAM-101 Paper ID : [ A1101 ]

## Time: 3 Hrs.

Max. Marks :60

2%.0

- *Note:-* (1) *Question-I is compulsory to attempt, Consisting of ten short answer type question carrying two marks each.* 
  - (2) Attempt five questions (carrying eight marks each) by electing at least two questions each form Section-A and Section B
- Q1. (a) Graph the set of points whose polar co-ordinates satisfy the conditions.

### $r \leq 0, \theta = \pi/4$

- (b) Obtain the local extreme values of the function  $f(x,y)=x^2+2xy$
- (c) Evaluate  $\iint_{0x}^{\pi\pi} \frac{\sin y}{y} dy dx$ .

d) If 
$$f(\mathbf{x},\mathbf{y}) = \sum_{n=0}^{\infty} (\mathbf{x}\mathbf{y})^n$$
, given  $|x\mathbf{y}| < 1$ , then find  $\frac{\partial f}{\partial \mathbf{x}}$ ,  $\frac{\partial f}{\partial \mathbf{y}}$ .

- (e)  $\vec{F}$  and  $\vec{G}$  are irrotational vector point functions, then show that  $\vec{F} \times \vec{G}$  is a solenoidal function.
- (f) State Stoke's Theorem.
- (g) If  $\vec{F} = \text{grad}(x^3 + y^3 + z^3 3xyz)$ , then find curl  $\vec{F}$
- (h) Find the work done by the force field  $\vec{F} = xy \hat{i} + (y-x)\hat{j}$  over the straight line from (1,1) to (2,3).
- (i) Rectify the curve  $x = acos^3 t, y = asin^3 t$ .
- (j) Find the possible percentage error in computing the resistance *r* from the formula (2x10=20)  $\frac{1}{r} = \frac{1}{r_1} + \frac{1}{r_2}$ , if  $r_1$  and  $r_2$  in error by 2%.

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### Section-A

- Q2. (a) Trace the curve  $x^3+y^3=3axy$  by giving all salient features in detail.
  - (b) Find the volume of the solid generated by the revolution of the curve  $r = a(1 + \cos\theta)$  about initial line. (5,3)
- Q3. (a) If  $\rho$  be the radius of curvature at any point P of the curve y<sup>2</sup>=4ax and S is its focus, then show that  $\rho^2$  varies as (SP)<sup>3</sup> (5,3)
  - (b) Find the area between the curve  $y^2(2a-x)=x^3$  and its asymptote.
- Q4. (a) Find the points on the surface  $z^2 = xy + 1$  nearest to the origin.
  - (b) Expand  $f(x,y) = \tan^{-1} xy$  in ascending powers of (x-1) and (y-1) up to second degree terms. (4,4)
- Q5. (a) If  $u = \tan^{-1} \frac{x^3 + y^3}{x y}$ , then prove that  $x^2 \frac{\partial^2 u}{\partial x^2} + 2xy \frac{\partial^2 u}{\partial x \partial y} + y^2 \frac{\partial^2 u}{\partial y^2} = 2 \sin u \cos 3u$

(b) If 
$$u = \log (x^3 + y^3 + z^3 - 3xyz)$$
, then prove that  
 $\left(\frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z}\right)^2 u = -9(x + y + z)^{-2}$   
Section-B  
(a) Using triple integral find the volume of the tetrahedron bounded by the co-ordinate planes and the plane  $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ 

(b) Evaluate :  $\iint_{0x^2}^{12-x} xy \, dxdy$  by changing the order of integration. (4,4)

Q7. (a) Prove that Curl (Curl 
$$\vec{F}$$
) = grad (div $\vec{F}$ ) - $\nabla^2$ 

(b) If  $\vec{F} = yz\hat{i} - xz\hat{j} + xy\hat{k}$ , then evaluate  $\iint_{S} \vec{F} \cdot \hat{N} \vec{B}s$ , where S is the portion of the surface of the sphere  $x^2 + y^2 + z^2 = 1$ , in the first octant. (3,5)

Q8. (a) Apply Stoke's theorem to evaluate the line integral  $\int_{c} [ydx+zdy+xdz]$ , Where C is the curve of intersection of the sphere  $x^{2}+y^{2}+z^{2}=a^{2}$  and the plane x+z=a.

(b) Using Green's theorem evaluate the line integral  $\int_{c} [(y-sinx)dx + cosxdy]$ 

Where C is the plane triangle bounded by the lines y=0,  $x=\pi/2$ ,  $y=(2/\pi)x$ 

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- (a) Verify Divergence theorem for  $\vec{F} = (x^2 yz)\hat{i} + (y^2 xz)\hat{j} + (z^2 xy)\hat{k}$  Taken over the **Q**9. rectangular parallelepiped  $0 \le x \le a, 0 \le y \le b, 0 \le z \le c$ .
  - (b) Evaluate  $\iint_{R} e^{x^2+y^2} dxdy$ , where R is semicircular region bounded by the x-axis and the curve  $y=\sqrt{1-x^2}$ , by changing to polar co-ordinates. (5,3)

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